

On Progress by DBD Collaboration

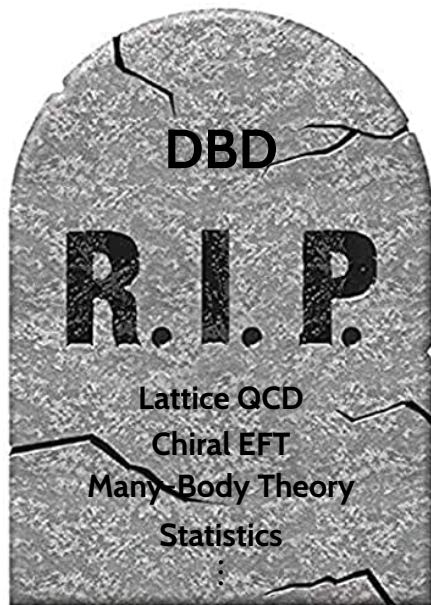
J. Engel

September 21, 2021

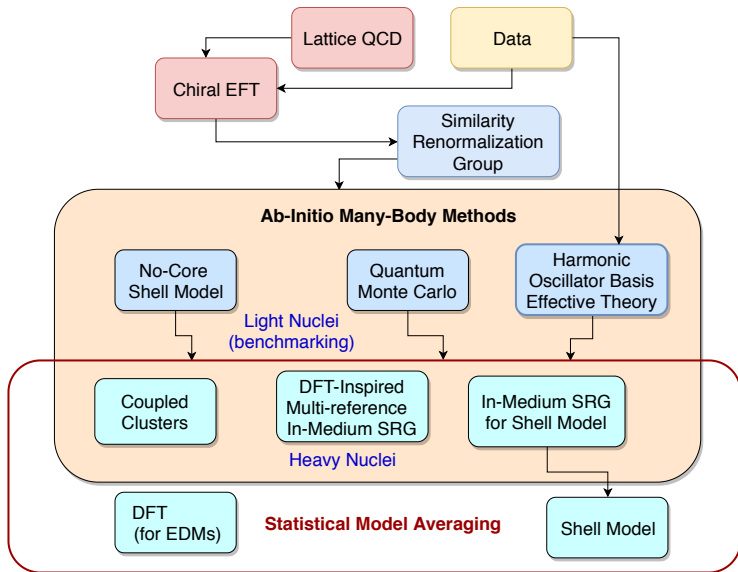


DBD Topical Theory Collaboration

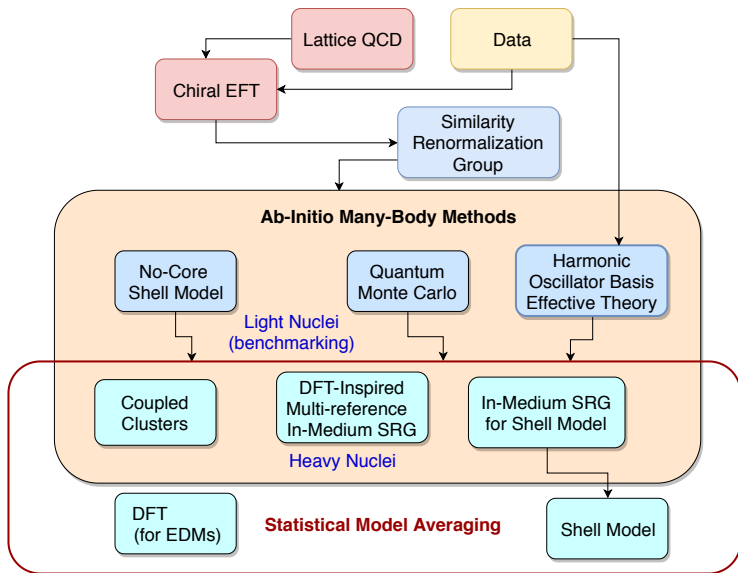
2016-2021



DBD Original Idea

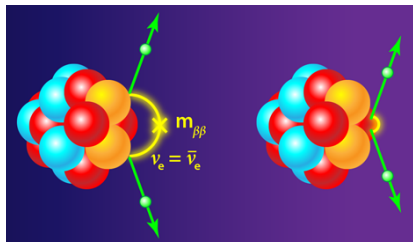


DBD Original Idea



A lot of this actually got done! And other unforeseen things as well!

The Problem

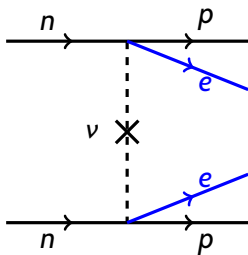


Rate depends on squares of unknown nuclear matrix elements. We need to compute them and assign a believable uncertainty so that experimentalists can

1. plan their experiments
2. draw conclusions from their results

EFT

Example: Light- ν Exchange at Leading Order

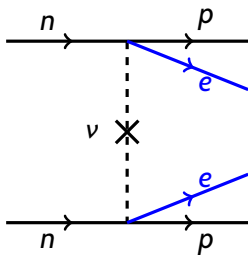


Usual long-range exchange

Almost all calculations so far include only this.

EFT

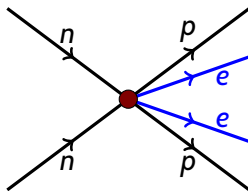
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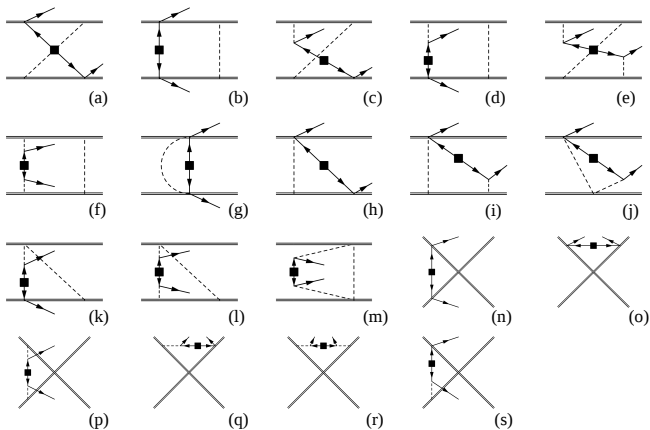
+



Contact counter term from short short-range exchange at energies beyond breakdown scale of EFT.

Constant in front now estimated.

Corrections of order 10% to standard diagram:



Size of effects confirmed in QMC calculations. Some coefficients still undetermined.

EFT

More...

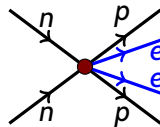
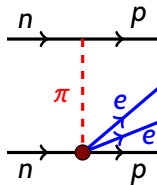
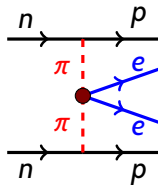
- ▶ EFT treatment of decay mediated by heavy-particle exchange
- ▶ Examination of effects of sterile neutrinos
- ▶ Synthesis of all possible operators and phase-space factors through “master formula”
- ▶ $\vdots$

Lattice QCD and Determination of Coefficient in χ EFT

Heavy-Particle Exchange

Effective field theory lists pion-nucleon-level operators and determines their importance.

Lattice QCD can compute dependence of blobs on new particle masses and couplings.

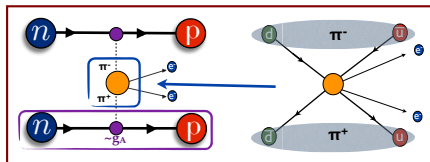
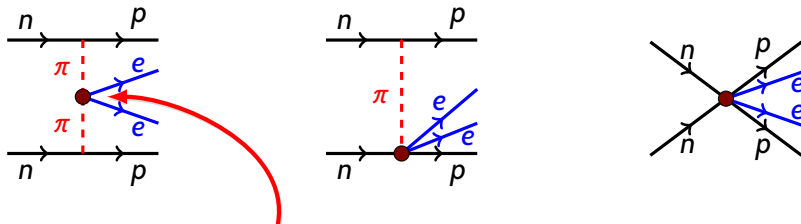


Lattice QCD and Determination of Coefficient in χ EFT

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Lattice QCD

Light- ν Exchange

Need

- ▶ Development of good two-nucleon operators (needed for heavy-particle exchange as well). Lots of activity here.
- ▶ Good treatment of massless fermions on lattice. QED effects can be studied to test methods.
- ▶ Lattice χ EFT for matching finite-volume LQCD results.

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- ▶ Lattice χ EFT for matching finite-volume LQCD results.

Lots of progress, but some of this is still a ways off.

Precise Estimate of g_A

nature

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A per-cent-level determination of the nucleon axial coupling from quantum chromodynamics

[C. C. Chang](#), [A. N. Nicholson](#), [E. Rinaldi](#), [E. Berkowitz](#), [N. Garron](#), [D. A. Brantley](#), [H. Monge-Camacho](#), [C. J. Monahan](#), [C. Bouchard](#), [M. A. Clark](#), [B. Joó](#), [T. Kurth](#), [K. Orginos](#), [P. Vranas](#) & [A. Walker-Loud](#) 

[Nature](#) **558**, 91–94 (2018) | [Cite this article](#)

Interlude: Light- ν Exchange in a Nucleus

$$[T_{1/2}^{0\nu}]^{-1} = G(Z, N) |M_{0\nu}|^2 \bar{m}_\nu^2$$

$$M_{0\nu} = M_{0\nu}^{GT} - \frac{g_V^2}{g_A^2} M_{0\nu}^F + M_{0\nu}^{\text{contact}} + \dots$$

with (at leading order in χ EFT)

$$M_{0\nu}^{GT} = \langle F | \sum_{i,j} H(r_{ij}) \boldsymbol{\sigma}_i \cdot \boldsymbol{\sigma}_j \tau_i^+ \tau_j^+ | I \rangle + \dots$$

$$M_{0\nu}^F = \langle F | \sum_{i,j} H(r_{ij}) \tau_i^+ \tau_j^+ | I \rangle + \dots$$

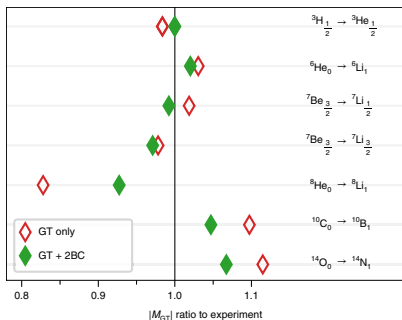
$$H(r) \approx \frac{2R}{\pi r} \int_0^\infty dq \frac{\sin qr}{q - (E_i + E_f)/2} \quad \text{roughly } \propto 1/r$$

Corrections are from “tensor” term. Higher-order terms in χ EFT also add stuff.

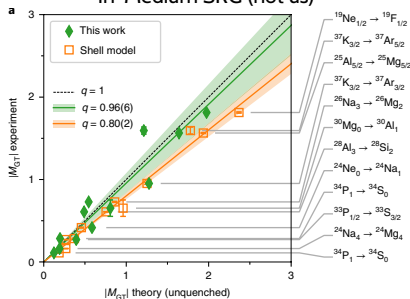
Explorations in Light Nuclei

g_A Quenching, Etc.

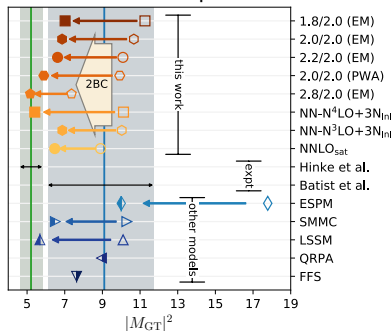
Quantum Monte Carlo



In-Medium SRG (not us)



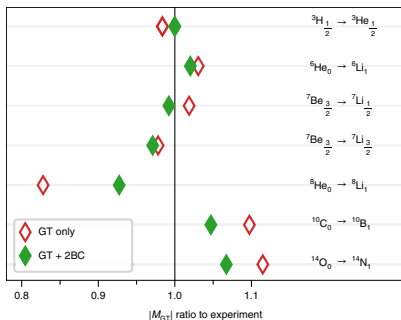
${}^{100}\text{Sn}$ in Coupled Clusters



Explorations in Light Nuclei

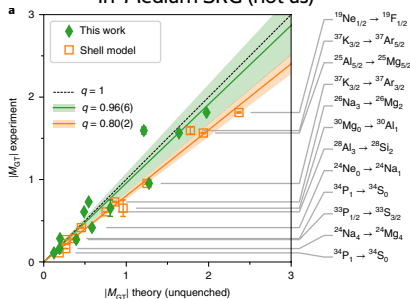
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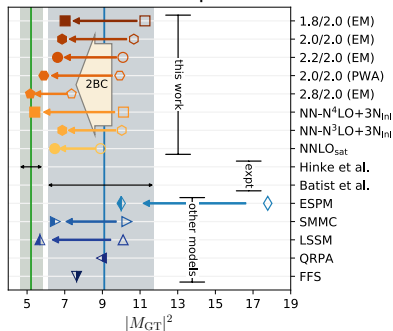


OK, ${}^{100}\text{Sn}$ is not so light...

In-Medium SRG (not us)

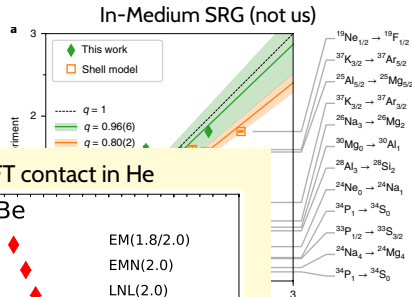


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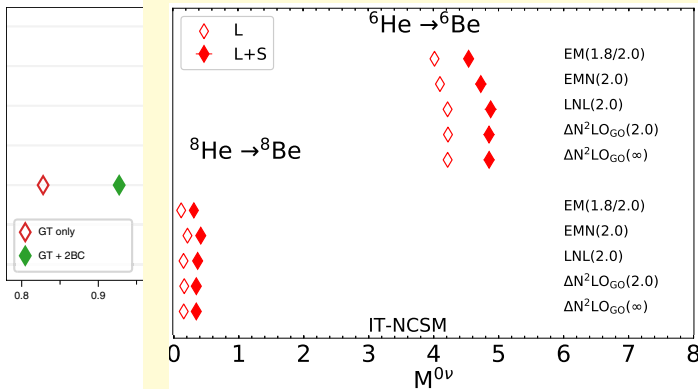
Explorations in Light Nuclei

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Qua

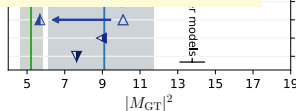
Test of effects of EFT contact in He



usters

1.8/2.0 (EM)
 2.0/2.0 (EM)
 2.2/2.0 (EM)
 2.0/2.0 (PWA)
 2.8/2.0 (EM)
 NN- $N^4\text{LO}+3N_{\text{Inl}}$
 NN- $N^3\text{LO}+3N_{\text{Inl}}$
 NNLO_{sat}
 Hinke et al.
 Batist et al.
 ESPM
 SMMC
 LSSM
 QRPA
 FFS

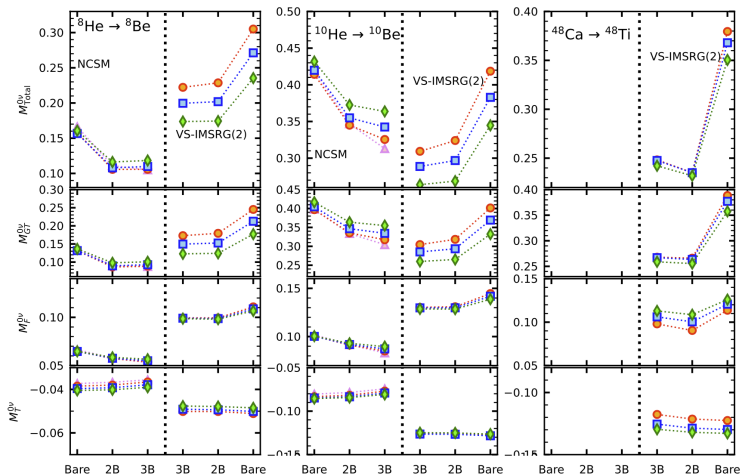
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Explorations in Light Nuclei

Softening of Operators with Similarity Renormalization Group

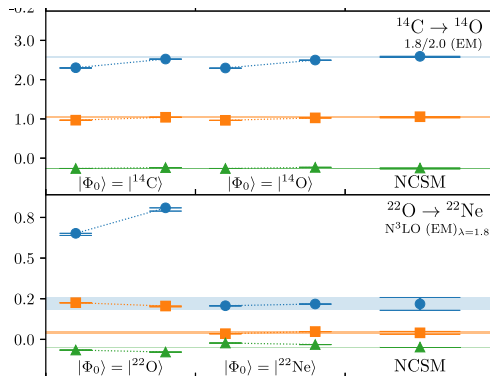
Produces operators for use in truncated single-particle spaces.



Explorations in Light Nuclei

Benchmarking of Methods

Quantum Monte Carlo and No Core Shell Model used to test the *ab initio* methods used in heavy nuclei and the phenomenological Shell Model.

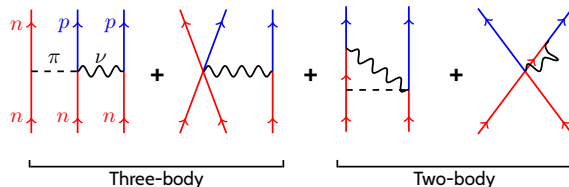


Comparison of Coupled Clusters and NCSM

Phenomenological Shell-Model in Heavy Nuclei

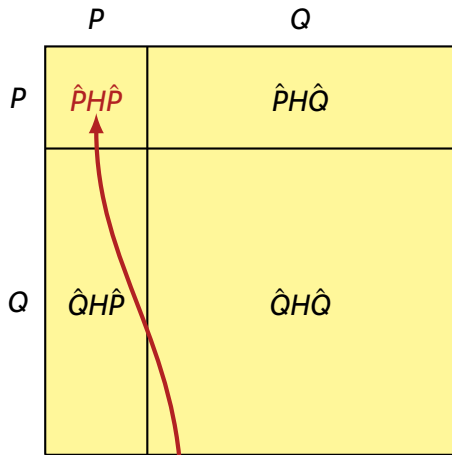
Used to

- ▶ Explore effectiveness of Generator Coordinate Method, a mixing of collective mean-field states at the heart of one *ab initio* method.
- ▶ Explore heavy-particle exchange in extensions of the Standard Model, opening-angle dependence of decay rates, etc.
- ▶ Explore the effects on light- ν exchange of the chiral two-body currents that help quench single- β decay (conclusion: they appear mild but an unknown contact term plays a role).



Ab Initio Many-Body Methods for Heavy Nuclei

Partition of Full Hilbert Space



P = subspace you want

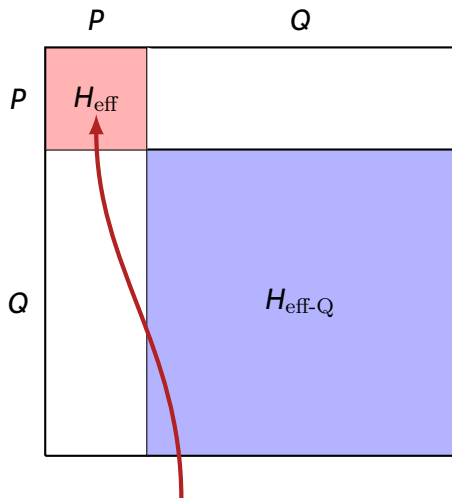
Q = the rest

Task: Find unitary transformation to make H block-diagonal in P and Q , with H_{eff} in P reproducing most important eigenvalues.

Simpler calculation done here.

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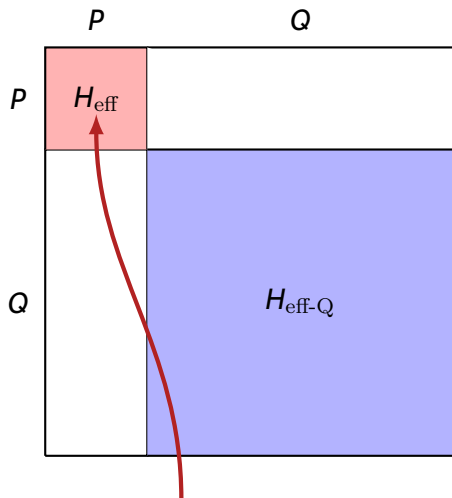
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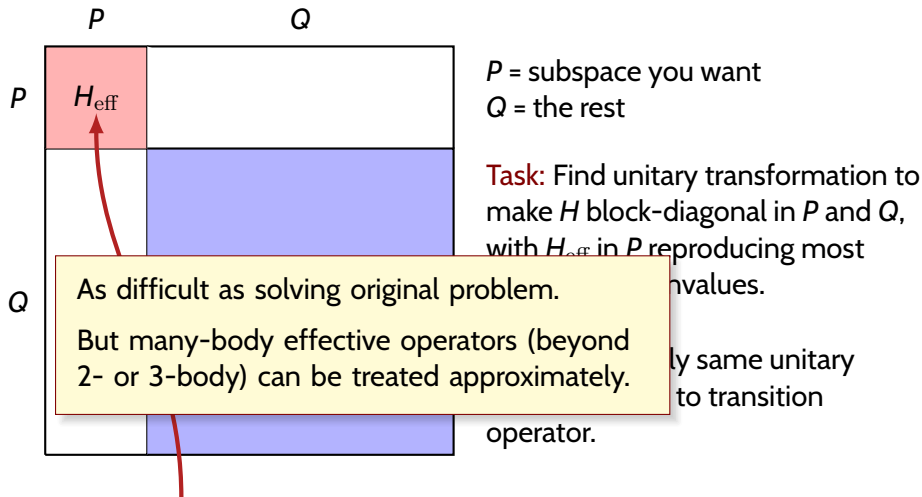
Task: Find unitary transformation to make H block-diagonal in P and Q , with H_{eff} in P reproducing most important eigenvalues.

Must must apply same unitary transformation to transition operator.

Simpler calculation done here.

Ab Initio Many-Body Methods for Heavy Nuclei

Partition of Full Hilbert Space

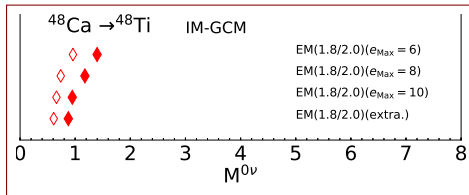
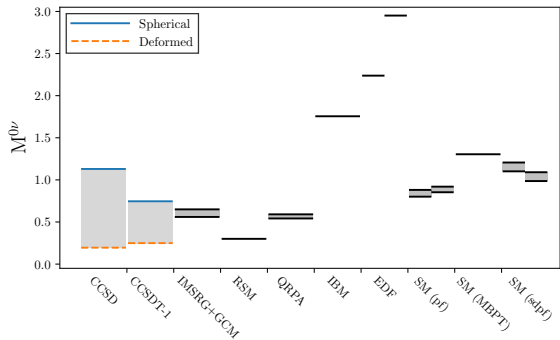


Simpler calculation done here.

Ab Initio Light- ν -Exchange Matrix Elements for ^{48}Ca

In-Medium Generator Coordinate Method and Coupled Clusters

Comparison of
all methods



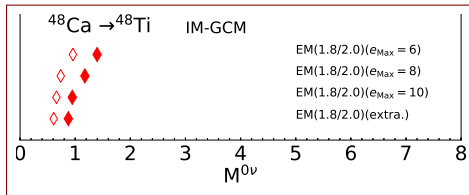
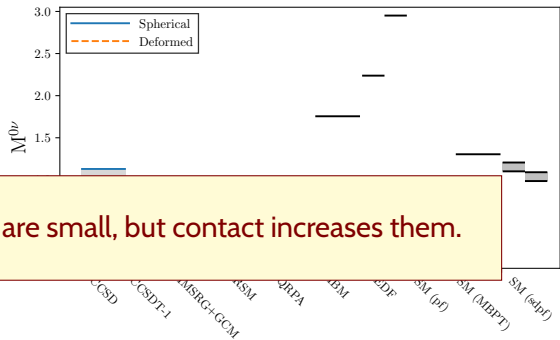
Effect of contact
in IM-GCM

Ab Initio Light- ν -Exchange Matrix Elements for ^{48}Ca

In-Medium Generator Coordinate Method and Coupled Clusters

Comparison of
a

Matrix elements are small, but contact increases them.



Effect of contact
in IM-GCM

Heavier Elements

- ▶ ^{76}Ge in progress in IM-GCM. Preliminary small-model space results on arXiv; agree pretty well with those of valence-space IMSRG.
- ▶ ^{130}Te , ^{136}Xe “in contemplation.”

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Perhaps ^{100}Mo should be next?

Uncertainty Quantification

We met a few times over Zoom towards the end of the collaboration and came up with a procedure that is on the conference website. A few people calculated a few related observables, but we never built up the steam to make a real dent in the problem.

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That's next!